

A2T

Example 4 page 55

Remember that

$$x^{-3} = \frac{1}{x^3}$$

Definition 3 page 53.

How do we show this? Take the term  $x^{-3}$  and multiply it by  $\frac{x^3}{x^3}$  .... Which is the same term with the positive exponent over itself. Since this is equal to 1, we can do that.. So we get

$$x^{-3} = x^{-3} \left( \frac{x^3}{x^3} \right) = \frac{x^{-3} x^3}{x^3} = \frac{x^{(-3+3)}}{x^3} = \frac{x^0}{x^3} = \frac{1}{x^3}$$

Now Example 4 is the same thing – just a little more complex.

$$\frac{(1+x^2)^{1/2}(2x) - x^2 \left( \frac{1}{2} \right) (1+x^2)^{-1/2}(2x)}{1+x^2}$$

To get the term  $(1+x^2)^{-1/2}$  into the denominator (and therefore have a positive exponent) they multiply the WHOLE thing by the conjugate (opposite exponent sign) – or

$$\frac{(1+x^2)^{1/2}}{(1+x^2)^{1/2}}$$

Which gives us

$$\frac{(1+x^2)^{1/2}(2x) - x^2 \left( \frac{1}{2} \right) (1+x^2)^{-1/2}(2x)}{1+x^2} * \frac{(1+x^2)^{1/2}}{(1+x^2)^{1/2}}$$

Then in the other steps they just multiply things out.